CS458 Assignment 3

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Question 1

1a)

The XOR of the two plaintexts is equivalent to the XOR of the two ciphertexts.

1b)

Question 2

2a)

Bob’s secret key is a = 23

Alice’s secret key is b = 58

Alice gives to Bob the value A = ga mod p = 523 mod 83 = 19

Bob gives to Alice the value B = gb mod p = 558 mod 83 = 7

s = Ba mod p = 723 mod 83 = **37**

s = Ab mod p = 1958 mod 83 = **37**

Without divulging their secret keys, Alice and Bob were able to arrive at the same value s. S would be the secret key shared between the two parties.

2b)

Note that Ba mod p is really (gb mod p)a mod p = gab mod p and Ab is really (ga mod p)b = gab mod p.

Eve knows g, ga and gb, she needs to find the value of gab to obtain the secret key.

To find a, Eve would have to compute logg(A) = b. For certain groups of G, the discrete log can be quickly computed but if G is chosen properly it would be extremely difficult as there is no efficient way of solving for b.

Hence, Eve can recover the original secret values provided that G is not properly chosen. It is difficult to recover if G is chosen properly.

2c)

Alice ---- Mallory ---- Bob

Alice sends ga mod p. Mallory intercepts and replaces ga with gm.

Bob sends gb mod p. Mallory intercepts and replaces gb with gm.

Neither Alice or Bob knows that the values they received were altered by Mallory.

Mallory then computes (ga mod p)b mod p which is the secret key with Alice and (gb mod p)a which is the secret key with Bob.

When Alice sends messages to Bob, Mallory is able to decrypt the message since Alice shares a secret key with Mallory and not with Bob directly. The message can be altered and sent to Bob with the secret key shared by Mallory and Bob.

From Alice and Bob’s perspective, nothing appears fishy.

A simple way to prevent this is to let ga and gb be signed by a Certificate Authority so that its values can be checked upon receiving it to make sure it is authentic.

Question 3

3a)

n = 4g2ab + 2ga + 2gb + 1 = 2g (2gab + a + b ) + 1

3b)

3c)

Question 4

a)

**Assumption**

Values of one column must be at least binary in nature like gender so that we can select two different groups.

**Tracker**

T = SELECT SUM (Salary) From Employee WHERE Gender = “F”

**Query**

q(C or T) = SELECT SUM (Salary) From Employee WHERE Name = “Cori” OR Gender = “F”

q(C or not T)

SELECT SUM (Salary) From Employee WHERE Name = “Cori” OR Gender <> “F”

q(S) = SELECT SUM (Salary) From Employee

Cori salary = q(C or T) + q(C or not T) – q(S)

4b)

**TARGET is the salary that we are guessing Rachel will have.**

q( C or T ) = SELECT COUNT(\*) FROM Employee WHERE Name = “Rachel” AND Salary = TARGET OR Gender = “F”

q(C or not T) = SELECT COUNT(\*) FROM Employee WHERE Name = “Rachel” AND Salary = TARGET OR Gender <> “F”

q(S) = SELECT COUNT(\*) FROM Employee WHERE Salary >= 0

q (C) = q(C or T) + q (C or not T) – q(S)

If q(C) = 2 i.e. COUNT returns 2, that means our guess was correct.